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# Integration of PD-type Iterative Learning Control with Adaptive Sliding Mode Control

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**Abstract:** Proportional-Derivative type Iterative Learning Controller (PD-ILC) is combined with an Adaptive Sliding Mode Controller (ASMC) using a plug-in structure to a rotary pendulum. The ASMC adaptation law is used to update a switching gain of sliding surface in Sliding Mode Control (SMC) controller. The proposed hybrid controller stability and convergence are mathematically shown and then experimentally demonstrated using two-degree-of-freedom (2-DOF) Quanser© QUBE<sup>TM</sup> Servo 2 Rotary Pendulum. Results illustrate that adaptation law helps the controllers to achieve higher accuracy tracking performance compared to the classic SMC controller. Based on the experimental results, the hybrid control of PD-ILC and ASMC has faster and more accurate tracking results than ILC controller indicating the combined controller has better performance than the individual controllers.

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*Keywords:* Iterative Learning Control; Sliding Mode Control; Adaptive Control; Robotic Pendulum; Hybrid Control

# 1 Introduction

Iterative Learning Control (ILC) is a control method that uses previous cycle information to learn how to control a system which has repetitive dynamics (Owens, 2015). For example in the industrial automation robotic manipulators repeat a certain action or motion. Each repeating action is called a "cycle," and the ILC controller uses error and control input from the previous cycle to learn the control input of upcoming cycle. The learning procedure in ILC is similar to humans learning a task where they gain skill by repeating it. Learning a new language is an example of skills that humans learn by repeating it over time. ILC has a simple structure which is computationally inexpensive and easy to design. Also, the model-free design has low complexity which is useful for real-time implementation and when it is difficult to model the system with high accuracy. Additionally, it has the potential to achieve perfect tracking by using a "non-causal" control signal (Xu et al., 2008).

Different types of ILC controllers have been used in literature such as proportional type ILC (P-type ILC) (Slepicka and Koch, 2016), proportional-derivative type (PD-type ILC) (Liu and Ruan, 2018), and proportional-integral-derivative type (PIDtype ILC) (Kim and Kim, 1996). ILC has been implemented on a wide variety of systems. Dual-loop D-type ILC law was used to control a flapping wing Micro Aerial Vehicle under distributed disturbances (He et al., 2018). ILC was designed for a class of nonlinear uncertain system, and the convergence of the controller was analyzed based on composite energy function (Xu et al., 2004). PD-type ILC was used to control a Multiple Flexible Manipulator Robot System, and the results showed that PD-type ILC is an effective method to obtain exact reference tracking (Dong et al., 2019). Adding a fuzzy mechanism to a PD-type ILC increased convergence speed of ILC and generalized it to be useful for different plants (Norouzi and Koch, 2019) and (Norouzi et al., 2019a). Errortracking iterative learning control was used to control a robot manipulator with random initial errors (Yan et al., 2019). In addition, ILC can be combined with conventional controllers as a plug-in hybrid controller to improve the performance of conventional controllers. Learning-based control using normoptimal iterative learning control with embedded PID controller was used to control soft robotic arm (Hofer et al., 2019).

Sliding Mode Controller (SMC) is a Lyapunov based controller which is designed based on the nonlinear system model (Khalil, 2002). This controller is robust and can overcome system uncertainty and input disturbances (Norouzi et al., 2019b). SMC was combined with different control laws such as adaptive control (Norouzi et al., 2018), Backstepping Control (Norouzi et al., 2019d), and Fuzzy Control (Jiang et al., 2018). Higherorder sliding surface (Amini et al., 2017) and integral sliding surface (Integral SMC) (Norouzi et al., 2019c) were used to control nonlinear systems. SMC has been integrated with iterative learning based sliding surface to enhance SMC tracking performance of wire tension of an automatic motor winding machine control (Lu et al., 2018). An adaptive law was combined with ILC to design output reference tracking control for a class of nonlinear plants (Yan et al., 2018). Adaptive ILC was combined with non-singular fast terminal sliding mode, and second-order SMC was used to increase convergence speed. The experiment using a 6-DOF robotic manipulator results in increasing in convergence of controller by using second-order SMC and ILC combination (Wu et al., 2018).

In this research, PD-type Iterative Learning control (PD-ILC) combined with an Adaptive Sliding Mode Controller (ASMC) using a plug-in structure is used. Convergence and stability of the ILC controller are mathematically analyzed, and stability of SMC and ASMC are checked based on Lyapunov stability theory. Compared to a classic ILC controller, the proposed ASMC-PD-ILC controller improves the performance resulting in fast and accurate reference tracking control. The proposed controller is used to control a 2-DOF Quanser© QUBE<sup>TM</sup> Servo 2 Rotary Pendulum.

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# 2 System Model

Consider the Multi-Input-Multi-Output (MIMO) system dynamic model which has *m* inputs and *p* outputs as

$$\ddot{q} = f(q, \dot{q}) + g(q) u, \tag{1}$$

where q is the generalized coordinate vector, u is the input vector as

$$q = [q_i]_{p \times 1} \quad i = 1, ..., p$$
  
$$u = [u_i]_{m \times 1} \quad j = 1, ..., m.$$
 (2)

Now *f* and *g* are introduced as the uncertainty as

$$f = [f_i]_{p \times 1} \quad i = 1, ..., p$$
  

$$g = [g_{ij}]_{p \times m} \quad i = 1, ..., p, \ j = 1, ..., m,$$
(3)

where it is assumed that the minimum and maximum of  $f_i$  and  $g_{ij}$  are known and can be calculated as  $f_i^-$ ,  $f_i^+$ ,  $g_{ij}^-$ , and  $g_{ij}^+$ . The estimation of these functions and error of estimation are  $\hat{f} = [\hat{f}_i]_{p \times 1}$ ,  $\hat{g} = [\hat{g}_{ij}]_{p \times m}$ ,  $\gamma = \gamma_{ij}$ ,  $F = [F_i]_{p \times 1}$  and  $G = [G_{ij}]_{p \times m}$  with the terms defined as

$$\hat{f}_{i} = \frac{f_{i}^{+} + f_{i}^{-}}{2}, \ \hat{g}_{ij} = \sqrt{g_{ij}^{+} g_{ij}^{-}}, \ \gamma_{ij} = \sqrt{\frac{g_{ij}^{+}}{g_{ij}^{-}}} \qquad (4)$$

$$F_i \ge |f_i^+ - \hat{f}_i| \text{ or } F_i \ge |\hat{f}_i - f_i^-|.$$

The system, linearized around a certain point, is defined in the state space form:

$$\dot{x}_{n\times 1} = A_{n\times n} x_{n\times 1} + B_{n\times m} u_{m\times 1}, \quad y_{p\times 1} = C_{p\times n} x_{n\times 1}, \quad (5)$$

where  $x_{n \times 1}$ ,  $y_{p \times 1}$ , and  $u_{m \times 1}$  are the model states, outputs, and inputs, respectively. The transfer function of system is calculated based on linearized system as

$$G_{sys}(s) = C[sI - A]^{-1}B,$$
 (6)

where  $G_{sys}$  is the  $p \times m$  transfer function matrix. For the remainder of the paper it is assumed the number of outputs equals the number of inputs (p = m).

#### 3 Sliding Mode Control

For the system Eq. 1, the sliding surface is selected as

$$s = (\lambda + \frac{d}{dt})e = \lambda e + \dot{e}, \tag{7}$$

where  $\lambda$  is diagonal matrix including  $\lambda_{ii}$  (i = 1, ..., p). The error vector of system is defined as

$$e = q - q_d \tag{8}$$

where  $e = [e_i]_{p \times 1}$  and  $q_d$  is the desired reference input. The best control law for sliding mode controller is achieved by setting the time derivative of sliding surface equal to zero (Slotine et al., 1991). The time derivative of Eq. 7 is

$$\dot{s} = \lambda \dot{e} + \ddot{e} = 0, \tag{9}$$

and substituting Eq. 8 into Eq. 9 and solving results in:

$$\lambda \dot{q} - \lambda \dot{q_d} + \ddot{q} - \ddot{q_d} = 0, \qquad (10)$$

where  $\ddot{q}$  can be find by substituting  $\hat{f}(q,\dot{q})$  and  $\hat{g}(q)$  into Eq. 1 as (Slotine et al., 1991)

$$\ddot{q} = \hat{f}(q, \dot{q}) + \hat{g}(q) u_{eq},$$
 (11)

where  $u_{eq}$  is a control input which makes the derivative of sliding surface equal to zero. Substituting Eq. 11 into Eq. 10 results in

$$\lambda \dot{q} - \lambda \dot{q_d} + \hat{f}(q, \dot{q}) + \hat{g}(q) \ u_{eq} - \ddot{q_d} = 0.$$
(12)

Taking  $u_{eq} = \hat{g}(q)^{-1}\hat{u}$  and solving Eq. 12 for  $\hat{u}$  results in

$$\hat{u} = -\lambda \dot{q} + \lambda \dot{q_d} - \hat{f}(q, \dot{q}) + \ddot{q_d}.$$
(13)

The sliding condition is defined as

$$\frac{1}{2}\frac{d}{dt}s^{T}s \le \eta ||s||, \tag{14}$$

where  $\eta$  is a strictly positive diagonal matrix  $\eta = [\eta_{ii}]_{p \times p}$ (Slotine et al., 1991). To satisfy the sliding condition, a switch term is added to  $u_{eq}$  as

$$u = u_{eq} - \hat{g}(q)^{-1} k \, sign(s), \tag{15}$$

where k is diagonal switching gain matrix. Now,  $k \ sign(s)$  is defined as a diagonal matrix

$$k \operatorname{sign}(s) = [k_{ii}]_{p \times p} [\operatorname{sign}(s_i)]_{p \times 1}.$$
 (16)

The sliding mode controller is obtained as

$$u_{SMC} = \hat{g}(q)^{-1} \bigg( -\lambda \dot{e} - \hat{f}(q, \dot{q}) + \ddot{q}_d - k \, sign(s) \bigg).$$
(17)

### 3.1 Adaptive Sliding Mode Control

An adaptive law can be added to update the switching gain based on the sliding surface (Norouzi et al., 2018) as

$$\hat{k}_{ii}(t) = \beta_{ii} |s_i(t)|, \ \hat{k}_{ii}(t|_{t=0}) = 0,$$
 (18)

where in the matrix format it can be defined as

$$\hat{k}(t) = \beta |s(t)|, \ \hat{k}(t|_{t=0}) = 0,$$
(19)

where  $\beta$  is the diagonal matrix of elements  $\beta_{ii}$ . So, the adaptive sliding mode controller is calculated as

$$u_{ASMC} = \hat{g}(q)^{-1} \left( -\lambda \dot{e} - \hat{f}(q, \dot{q}) + \ddot{q}_d - \hat{k} \beta \operatorname{sign}(s) \right), \quad (20)$$

where now  $\hat{k}$  is a function of time.

## 4 PD-type Iterative Learning Control (PD-ILC)

Iterative Learning Control is often defined as

$$u_{j+1}(t) = Q(u_j(t)) + L(e_j(t)),$$
(21)

where *L* is a learning filter, *Q* is a Q-Filter (Control input filter), and *j* is cycle index. Both *Q* and *L* are matrices with dimension of  $p \times p$ . If the learning filter has only constant values on the main diagonal elements of matrix, then a the P-type controller is generated. Taking *Q* to be a identity matrix results in (Ahn et al., 2007)

$$u_{i+1}(t) = u_i(t) + Le_i(t), \qquad (22)$$

where the current cycle control input is function of the previous cycle's error and control input. By modifying the matrix L a PD-type ILC controller is obtained as

$$u_{j+1}(t) = u_j(t) + Pe_j(t) + D\dot{e}_j(t), \qquad (23)$$

where *P* and *D* is the proportional and derivative learning gain, respectively (Ahn et al., 2007).

## 5 Hybrid Plug-in PD-type ILC with ASMC- ASMC-PD-ILc

The Plug-in ILC with parallel structure is (Lei et al., 2015)

$$u_j(t) = u_{ASMC,j}(t) + u_{PD-ILC,j}(t), \qquad (24)$$

where  $u_{ASMC,j}(t)$  is the ASMC controller,  $u_{PD-ILC,j}(t)$  is the PD-type ILC,  $u_j(t)$  is the combined control signal of the system, and *j* is iteration cycle. The proposed hybrid controller block diagram is shown schematically in Fig. 1. Substituting Eq. 23 and 20 into Eq. 24 the hybrid control law is calculated as

$$u_{j} = \hat{g}^{-1}(q_{j}) \left( -\lambda \dot{e}_{j} - \hat{f}(q_{j}, \dot{q}_{j}) + \ddot{q}_{d} - \hat{k} \beta sign(s_{j}) \right)$$
  
+  $u_{j-1} + Pe_{j-1} + D\dot{e}_{j-1}.$  (25)

To avoid chattering, a saturation function with constant boundary layer is used instead of the  $[sign(s_i)]_{p \times 1}$  function as

$$sat(\frac{s_{i}}{\phi}) = \begin{cases} 1 & \frac{s_{i}}{\phi} > 1\\ \frac{s_{i}}{\phi} & -1 < \frac{s_{i}}{\phi} < 1 & i = 1, ..., n\\ -1 & \frac{s_{i}}{\phi} < -1 \end{cases}$$
(26)

#### 6 Stability Analysis

# 6.1 Stability Analysis of ILC controller

The term  $Q - G_{sys}L$  is used as the stability criteria to analysis the stability of an ILC controller for a linear system. So, for ILC asymptotic stability, a necessary but not sufficient conditions for this case is defined as

$$||Q - G_{sys}L||_{\infty} < 1,$$
 (27)

or  $\bar{\sigma}(Q - G_{sys}L) < 1$  where *L* is a diagonal matrix and  $G_{sys}$  is a symmetric matrix, and  $\bar{\sigma}$  is a maximum singular value (Owens, 2015). Monotonic convergence occurs when  $\bar{\sigma}(M) < 1$  where  $M = [Q - G_{sys}(s)L]$  in  $e_{j+1} = Me_j$ . Using the same concept for convergence and stability analysis of P-type ILC, the stability and convergence criteria for PD-type ILC can be calculated as

$$e_{j+1} = q_d - y_{j+1} = r - G_{sys}u_{j+1} = q_d - G_{sys}Qu_j - G_{sys}Pe_j - sG_{sys}De_j.$$
(28)

So, by assuming that the Q-filter equals to identity matrix, M is calculated as

$$e_{j+1}(s) = [I - G_{sys}(s)(P + sD)]e_j(s).$$
(29)

Thus, for the PD-type controller stability and convergence conditions are

$$\bar{\sigma}(I - G_{sys}(s)(P + sD)) < 1. \tag{30}$$

The second norm of error can be calculated as

$$||e_{q(j)}||_2 = \sqrt{e_{q(j)}^* e_{q(j)}},\tag{31}$$

where j is the repetitive cycle number and  $e_q$  is the tracking error vector of q in Eq. 8.

# 6.2 Adaptive Sliding Mode control

To establish the sliding condition (Eq. 14), the range of k is found to be

$$k \ge \gamma \left(F + \eta\right) + \left(\gamma - I\right) \left|\hat{u}\right|,\tag{32}$$

where this equation is obtained based on Lyapunov stability theorem (Slotine et al., 1991) for SMC. For the stability analysis of ASMC a candidate Lyapunov function is defined as

$$V(t) = \frac{1}{2}s^{T}s + \frac{\hat{g}^{-1}g}{2}\tilde{k}^{T}\tilde{k},$$
(33)

where  $\tilde{k}$  is defined as

$$\tilde{k} = \hat{k} - k. \tag{34}$$

Taking the time derivative of candidate Lyapunov function (Eq. 33) and substituting the system dynamic model (Eq. 1) and ASMC control law (Eq. 20) results in

$$\begin{split} \dot{V}(t) &= s\dot{s} + \hat{g}^{-1}g\tilde{k}\tilde{k} \\ &= s(\ddot{q} - \ddot{q}_d + \lambda\dot{e}) + \hat{g}^{-1}g(\hat{k} - k)\beta|s| \\ &= s(f + gu - \ddot{q}_d + \lambda\dot{e}) + \hat{g}^{-1}g(\hat{k} - k)\beta|s| \\ &= s(f + g\hat{g}^{-1}(-\lambda\dot{e} - \hat{f} + \ddot{q}_d - \hat{k}\beta\,sign(s)) \\ &- \ddot{q}_d + \lambda\dot{e}) + \hat{g}^{-1}g(\hat{k} - k)\beta|s| \\ &= s(f - \hat{f} + \hat{f} + g\hat{g}^{-1}(-\lambda\dot{e} - \hat{f} + \ddot{q}_d - \hat{k}\beta\,sign(s)) \\ &- \ddot{q}_d + \lambda\dot{e}) + \hat{g}^{-1}g(\hat{k} - k)\beta|s| \\ &= s((f - \hat{f}) + (g\hat{g}^{-1} - 1)(-\hat{f} + \ddot{q}_d - +\lambda\dot{e}) \\ &- g\hat{g}^{-1}\hat{k}sign(s)) + g\hat{g}^{-1}(\hat{k} - k)\beta|s|. \end{split}$$

simplifying using the triangle inequality and using Eq. 4, results in

$$\dot{V}(t) \le |s||F| + |s||g\hat{g}^{-1} - 1||\hat{u}| - g\hat{g}^{-1}k\beta|s|.$$
 (35)

Based on Eq. 4,  $|1 - g\hat{g}^{-1}| \le |1 - \gamma^{-1}|$  and  $-g\hat{g}^{-1} \le -\gamma^{-1}$  are obtained. Then, substituting these into the Eq. 35 results in

$$\dot{V}(t) \le |s||F| + |s||1 - \gamma^{-1}||\hat{u}| - \gamma^{-1}k\beta|s|.$$
(36)

Finally, substituting Eq. 32 into Eq. 36, results in

$$\dot{V}(t) \leq |s||F| + |s||1 - \gamma^{-1}||\hat{u}| 
- \gamma^{-1}(\gamma (F + \eta) + (\gamma - I) |\hat{u}|)\beta|s| 
\leq ((I - \beta)(F + |I - \gamma^{-1}||\hat{u}|)|s|) - \eta\beta|s|.$$
(37)

So, if  $\beta_i \ge 1$  the time derivative of Lyapunov function would be  $\dot{V}(t) \le 0$ . So, the system is stable based on Lyapunov stability theory, if and only if  $\beta_i \ge 1$  for all *i*.

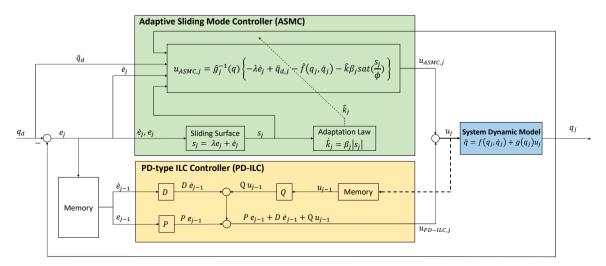


Fig. 1. Hybrid Adaptive Sliding Mode Control with PD-type Iterative Learning Control (ASMC-PD-ILC)

(38)

#### 7 Experiment Results and Discussion

To experimentally test the proposed controller, the Quanser $\bigcirc$  QUBE<sup>TM</sup> Servo 2 rotary pendulum is used. A schematic of system is shown in Fig. 2. Using the Euler-Lagrange method, the dynamic model of system is obtained as (Apkarian et al., 2016)

 $\begin{bmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{bmatrix} \begin{bmatrix} \ddot{\theta} \\ \ddot{\alpha} \end{bmatrix} + \begin{bmatrix} C_1 \\ C_2 \end{bmatrix} = \begin{bmatrix} T_1 \\ T_2 \end{bmatrix},$ 

where

$$M_{11} = m_p L_r^2 + \frac{1}{4} m_p L_p^2 - \frac{1}{4} m_p L_p^2 \cos(\alpha)^2 + J_r$$

$$M_{12} = \frac{1}{2} m_p L_p L_r \cos(\alpha), \quad M_{21} = \frac{1}{2} m_p L_p L_r \cos(\alpha)$$

$$M_{22} = J_p + \frac{1}{4} m_p L_p^2, \quad C_1 = \left(\frac{1}{2} m_p L_p^2 \sin(\alpha) \cos(\alpha)\right) \dot{\theta} \dot{\alpha}$$

$$+ \left(\frac{1}{2} m_p L_p L_r \sin(\alpha)\right) \dot{\alpha}^2 + \frac{k_m^2 \dot{\theta}}{R_m} + D_r$$

$$C_2 = -\frac{1}{4} m_p L_p \cos(\alpha) \sin(\alpha) \dot{\theta}^2 + \frac{1}{2} m_p L_p g \sin(\alpha) + D_p \dot{\alpha}.$$

The right hand of Eq. 38 is the input torque to the first and second link defined as  $[B_1 \ B_2]^T \ V_m$  where  $B_1 = K_m/R/m$  and  $B_2 = 0$ . The DC motor voltage  $(V_m)$  is control input (actuator dynamic is included) and rotary link angle ( $\theta$ ) and pendulum angle ( $\alpha$ ) are system outputs. The experimental setup using QUBE rotary Pendulum is shown in Fig. 3. Based on Eq. 38, the standard for of dynamic equation of motion (Eq. 1) as achieved where  $f(q, \dot{q}), g(q), q$ , and u are defined as

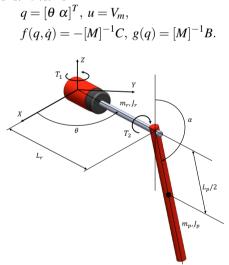


Fig. 2. kinematic diagram of the QUBE rotary pendulum



Fig. 3. Experiment setup of QUBE rotary pendulum

Fig. 4 shows the experimental results of SMC and ASMC controllers. In all experimental results a back and forth reference desired input is used as rotary desired angle ( $\theta$ ) and 180° reference desired input for pendulum angle ( $\alpha$ ). Reference tracking results of SMC versus ASMC show the adaptation law in the SMC controller results in more accurate reference tracking in Fig. 4. Adding an adaptive law decreases second norm of error for one single cycle from 18.74 for SMC to 12.43 for ASMC. The more accurate tracking of rotary angle ( $\theta$ ) using ASMC, the more oscillatory the pendulum angle ( $\alpha$ ). The experimental result of PD-ILC controller for repetitive reference of rotary angle ( $\alpha$ ) are shown in Fig. 5. In this test, a square Wave with amplitude of 20 degree and frequency of 0.0625 Hz is used as reference input and each period of this square wave is taken as a cycle for PD-ILC controller. As illustrated, after a 31 cycles, the controller can achieve acceptable tracking of desired reference. This is quantified by the second norm of error of each cycle versus number of iteration ( $||e_{\theta}||_2$  versus *j* plot in Fig. 5) where shows ILC monotonic convergence. The experimental results of reference tracking using Hybrid ASMC-PD-ILC controller are shown in Fig. 6. The reference input is the same as Fig. 5. For this case, the combined controller converges faster than pure ILC controller and second norm of the error decreases from 23.67 to 9.69.

As shown in Figs. 4-6, the damping between the joint of rotatory arm and pendulum is very low. Hence, by increasing the tracking accuracy and response time of the  $\theta$ , the oscillation on the  $\alpha$  increases. This is a trade-off between tracking the desired value of the  $\theta$  and stabilizing the pendulum ( $\theta = 180^{\circ}$ ). Based on Fig. 6, from cycle 1 to 7, oscillation is increased as the response time, and the accuracy of  $\theta$  tracking is increased. For the last four cycles, both oscillation, and  $\theta$  tracking stays unchanged. This can be analyzed based on the second norm of error ( $||e_{\theta}||$ ), as shown in Fig. 6. At convergence of the learning control, the performance remains unchanged as the reference is repeated with the same amplitude and frequencies. The same conclusion can be made for pure ILC controller as shown in Fig. 5.

To compare performance of different controller, the second norm of tracking error of last cycle is compared in Table 1. Also, the last cycle of system response for four kinds of controllers are shown in Fig. 7.

Table 1. Performance comparison of controllers

| Controller type | $  e_{\theta}  _2$ | Accuracy wrt SMC | Accuracy wrt ILC |
|-----------------|--------------------|------------------|------------------|
| SMC             | 18.74              | -                | -32.9%           |
| ASMC            | 12.43              | +33.7%           | +1.1%            |
| ILC             | 12.57              | +32.9            | -                |
| ILC with ASMC   | 9.68               | +48.3%           | +23%             |

Based on Table 1, it can be concluded that the proposed combined controller has faster convergence and more accurate reference tracking than PD-type ILC controllers. The proposed controller converges in 11 cycles while for pure ILC the convergence occurs in 31 cycles (64.5% faster). The combined controller is also an improvement on just the ASMC. The combination of ASMC-PD-ILC produces the best results when compared to the individual controllers.

## 8 Conclusion

A PD-type Iterative Learning Controller is combined with Adaptive Sliding Mode Controller and the stability and convergence of the proposed controller are analyzed. Then, a 2-DOF QUBE rotary pendulum is used to test the designed controllers

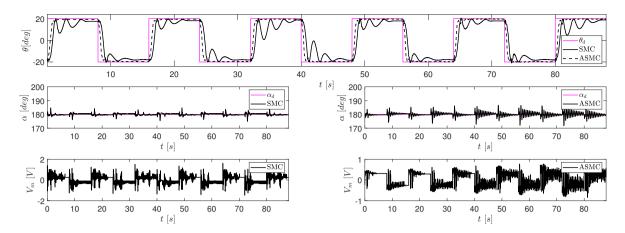


Fig. 4. Experimental results: reference tracking of QUBE rotary angle ( $\theta$ ) and stabilizing pendulum angle ( $\alpha$ ) using Sliding Mode Controller (SMC) versus Adaptive Sliding Mode Controller (ASMC)

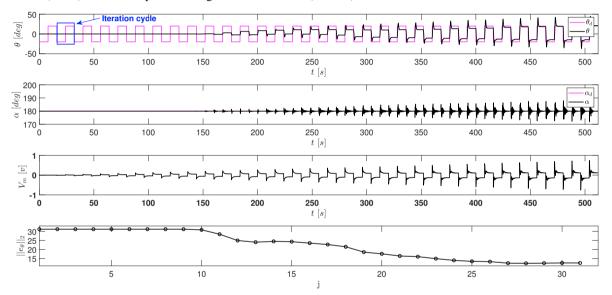


Fig. 5. Experimental results: reference tracking of QUBE rotary angle ( $\theta$ ) and stabilizing pendulum angle ( $\alpha$ ) using PD-type Iterative Learning Control (PD-ILC)

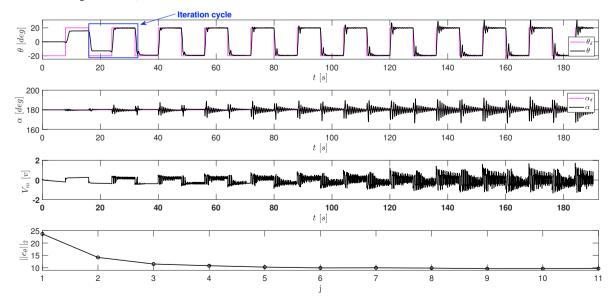


Fig. 6. Experimental results: reference tracking of QUBE rotary angle ( $\theta$ ) and stabilizing pendulum angle ( $\alpha$ ) using Hybrid Adaptive Sliding Mode Controller and PD-type Iterative Learning Control (ASMC-PD-ILC)

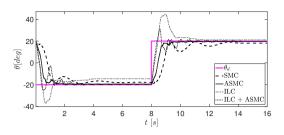


Fig. 7. Performance comparison of controllers - the last cycle of learning-based controller are considered for comparison

by comparing experimental results of SMC and ASMC, PD-ILC, and ASMC-PD-ILC. For this system several observation can be made. One, adding the adaptation law helps the hybrid controller to achieve more accurate tracking performance. Two, adding ASMC to PD-ILC improves system convergence speed and tracking performance. Three, as the ASMC controller is designed based on the model, it depends on the accuracy of the model; however, the proposed controller is able to compensate model mismatch of plant system model to improve tracking accuracy of the controller. This is clear by using adaptation and learning together. Understanding how the additional methods such as Backstepping Control, Model Predictive Control, and Optimal Control could be added to further improve the control performance is future research.

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